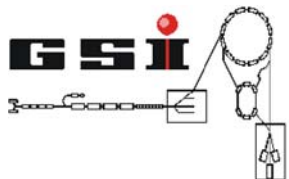




GICOSY Calculations for HRS

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DESIR HRS Meeting
Bordeaux, 17+18th Nov. 2011

- ❖ **Fringe Fields**
- ❖ **Hexapole Corrections**
- ❖ **Misalignments**





Fringe Fields + Effective Lengths

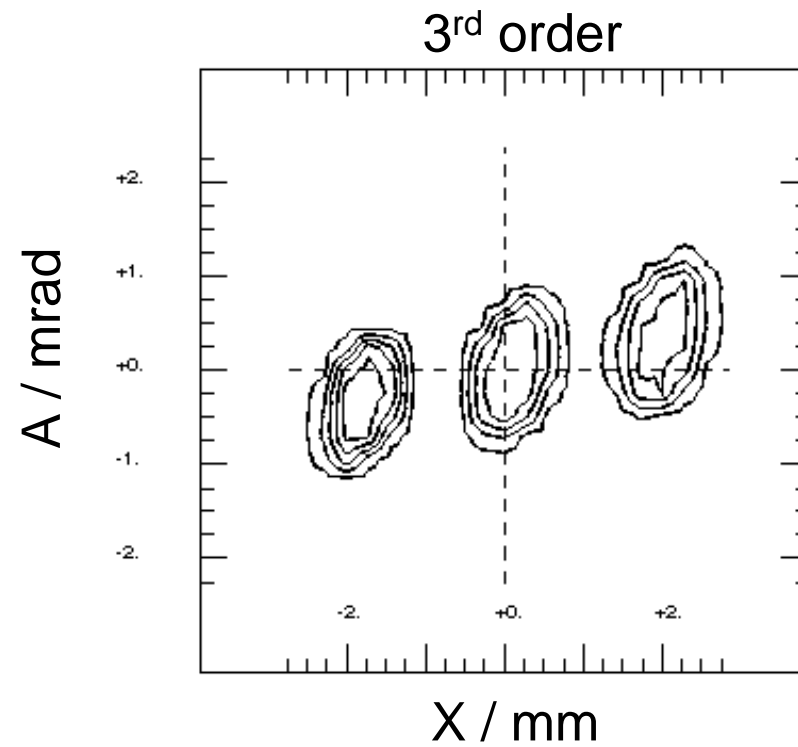
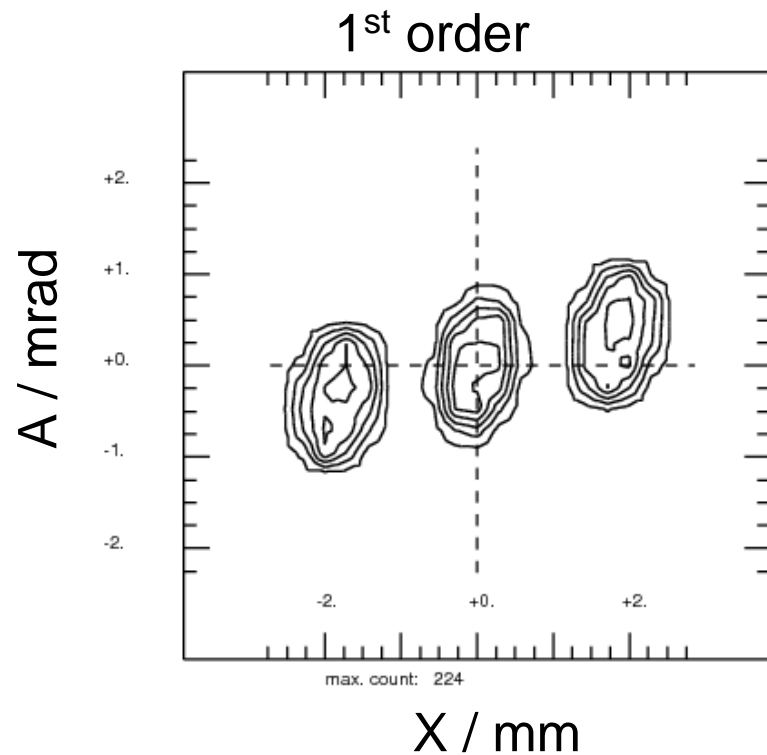
We still don't have the real FF distributions, but they can be calculated with SIMION or TOSCA.

Still the design is good enough because even assuming the largest possible variation of fringe field extension just requires a small readjustment of quadrupoles + multipole, and all optical properties are restored.

The effective lengths of quadrupoles and dipoles need to be calculated. They will differ from geometrical lengths. This effect is much larger than that coming from the fringe fields.

Phase Space after all Multipole Corrections

phase space $X_0 * A_0 = 0.5\text{mm} * 7\text{ mrad}$, $\delta_m = \Delta m/m = 1/20000$

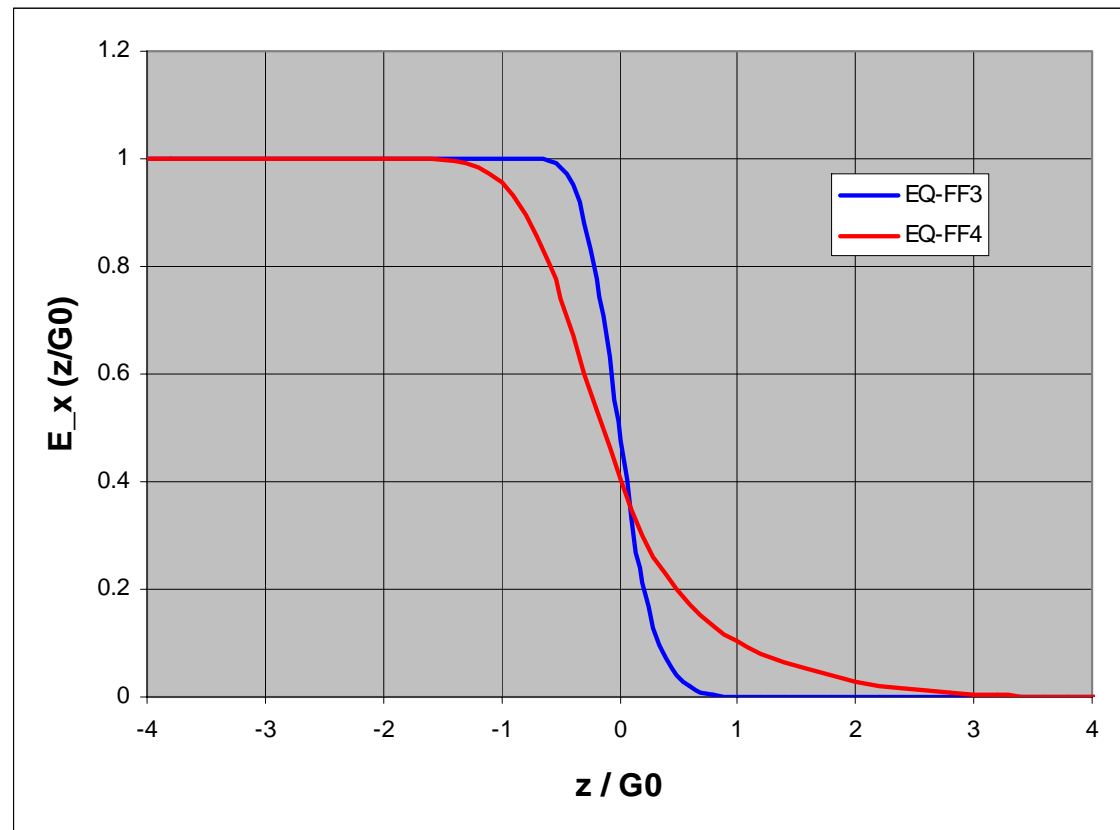


In perfect system

Just to verify the calculations

Possible Fringe Field Distributions

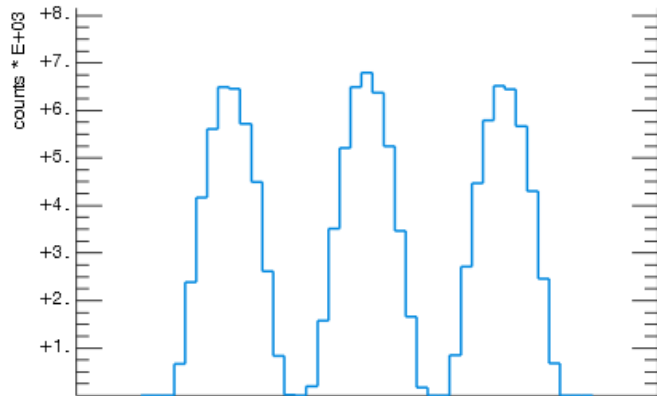
Two extreme cases for EQ from GICOSY list, **FF3** and **FF4**, different Enge coefficients (field shape) but same effective length (field integral).



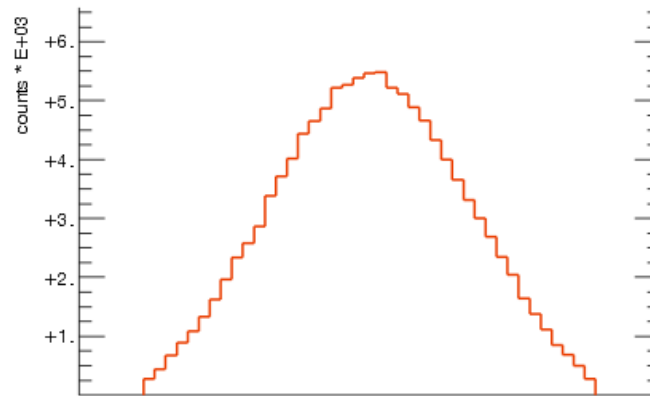
Depends much on environment: beam pipe, neighboring elements

At Image Plane

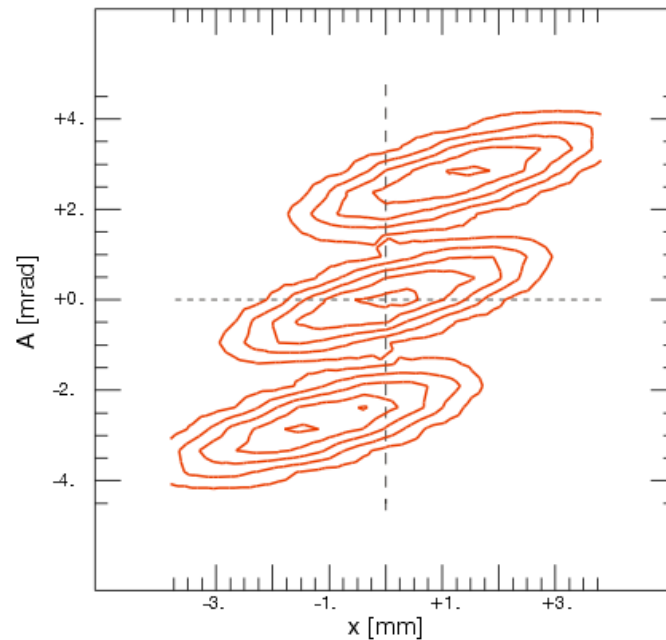
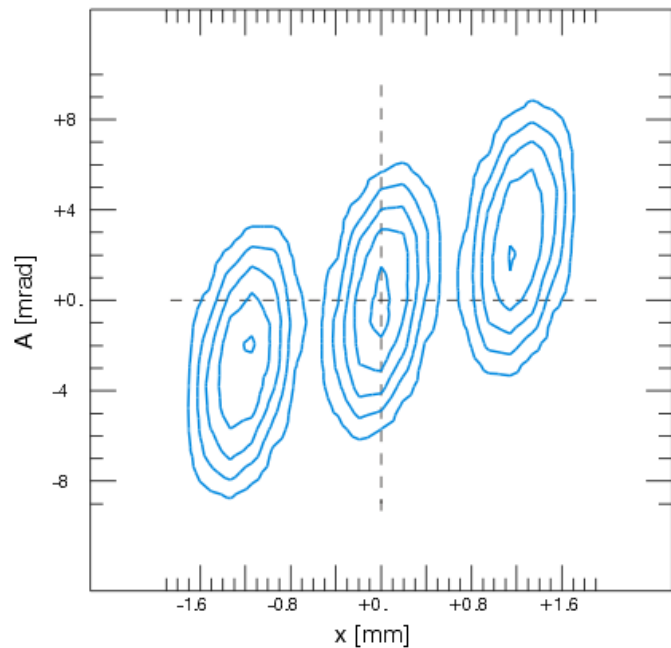
FF3 for all quads



FF4 for all quads

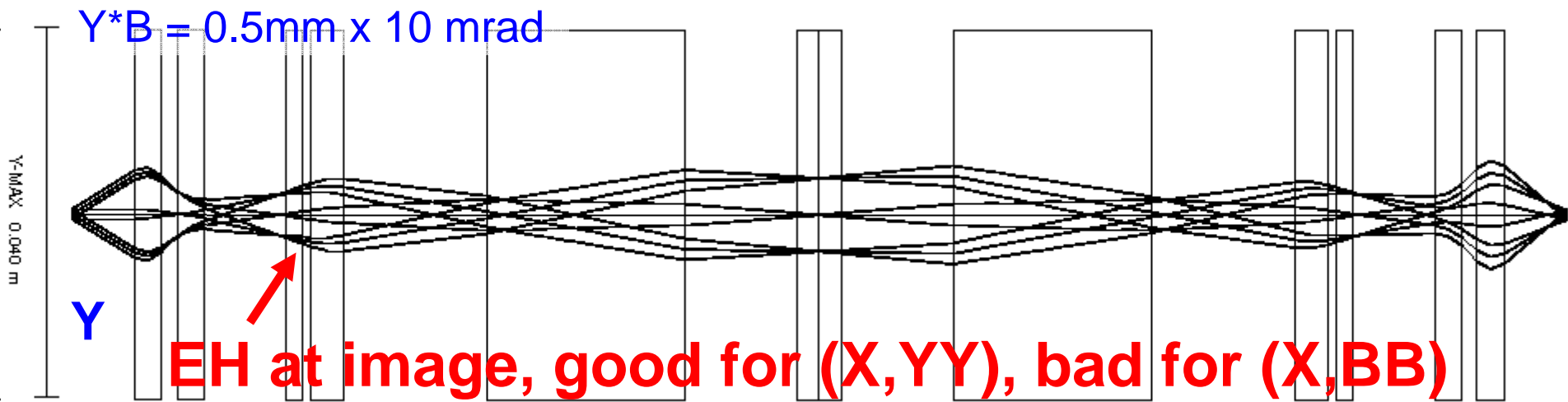
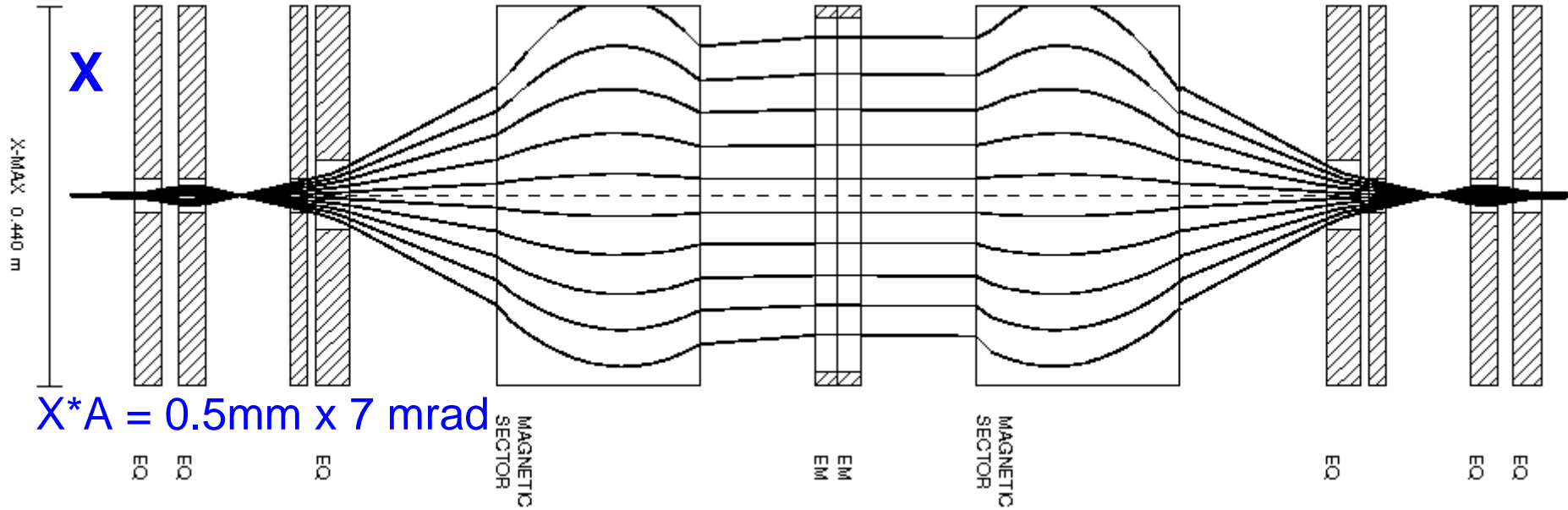


Shift of image plane $\Delta f_x = 2.9$ m, but with refit we get the same picture as before.



MQ1, + 1%
MQ2, +1%
FQ1, -2%

Trajectories (3rd order)



Effect of first and third Hexapole

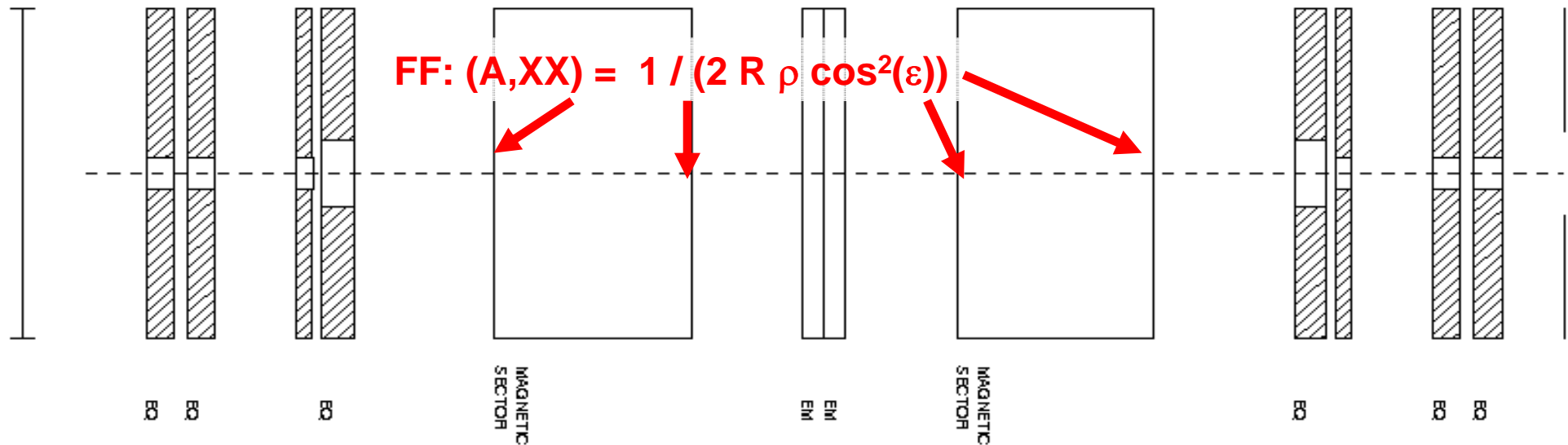
Assume symmetric operation,
but also opposite polarity checked, values for 60 keV

$U = 0.00 \text{ kV}, 0.00 \text{ kV}$	$\rightarrow (X, BB) = 1.17\text{m}, (X, YY) = 1237/\text{m}, (X, AA) = 0 \text{ m}$
$U = 0.10 \text{ kV}, 0.10 \text{ kV}$	$\rightarrow (X, BB) = 1.16\text{m}, (X, YY) = 895/\text{m}, (X, AA) = 54 \text{ m}$
$U = 0.10 \text{ kV}, -0.10 \text{ kV}$	$\rightarrow (X, BB) = 1.17\text{m}, (X, YY) = 1225/\text{m}, (X, AA) = 0 \text{ m}$
$U = 0.36 \text{ kV}, 0.36 \text{ kV}$	$\rightarrow (X, BB) = 1.14\text{m}, (X, YY) = 0/\text{m}, (X, AA) = 195 \text{ m}$

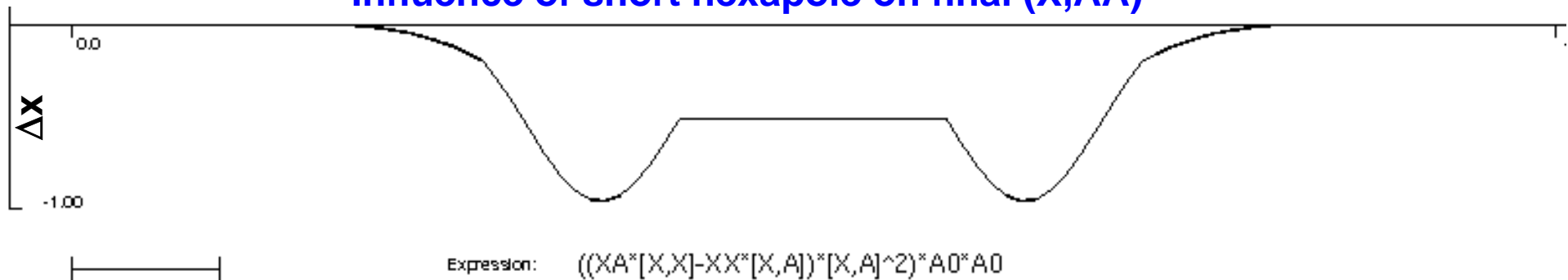
$\Rightarrow (X, YY)$ can be corrected (no small Y slit needed)
 (X, AA) needs only small retuning with central multipole

(X, BB) cannot be corrected,
but it is compensated by symmetry,
here $(X, BB) * B_0 * B_{0 \text{ max}} = 0.056 \text{ mm}$, with $B_0 = 7 \text{ mrad}$
requires large deviation from symmetry to be disturbing.

Coupling Coefficient for (X,AA)



Influence of short hexapole on final (X,AA)



Curvature = $\rho / R = 0.85\text{m} / 5.76\text{m}$ on all sides makes overall (X,AA) zero.

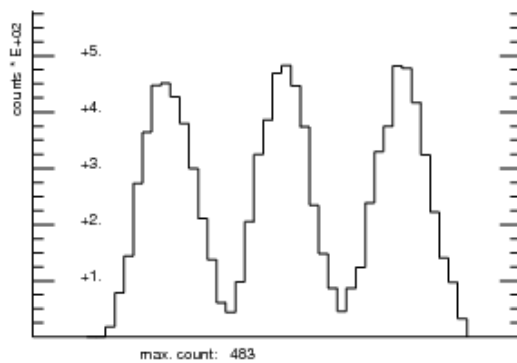
It may be easier to use only the much more sensitive inner sides.

R = 3m would overcorrect the aberration by far!

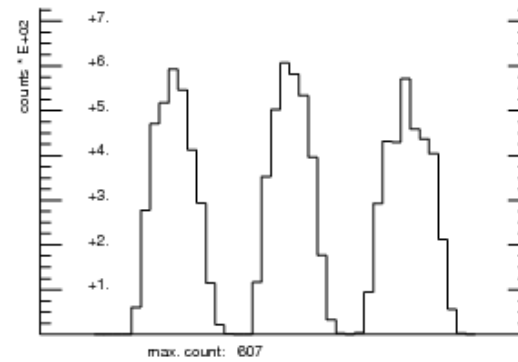
Phase space with some quads rotated a bit

3rd order GICOSY calculation

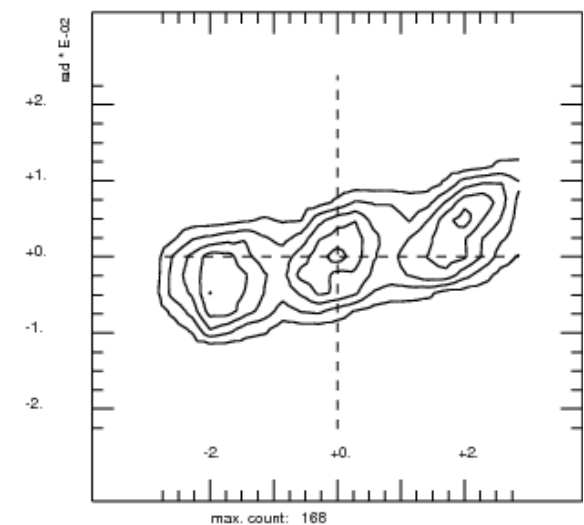
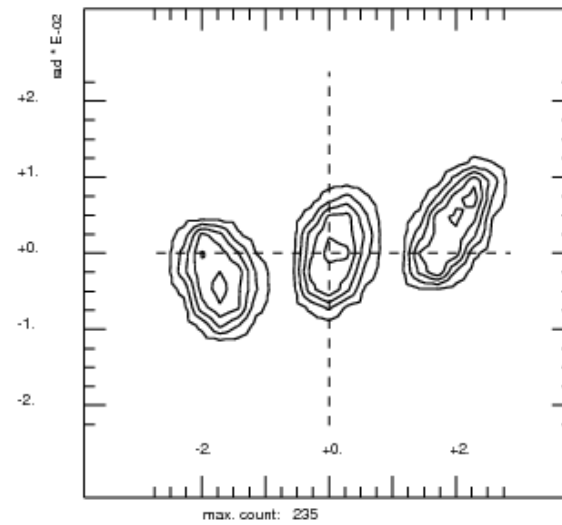
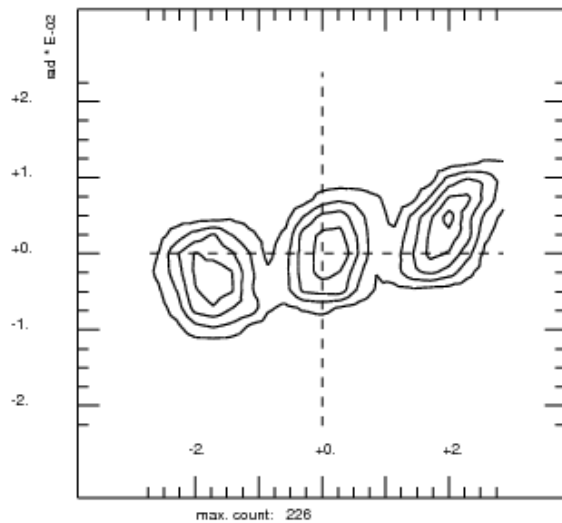
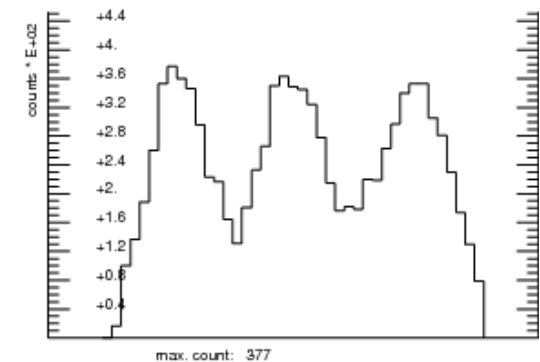
1st quad rot. by 1°



1st + 2nd quad rot. by 1°



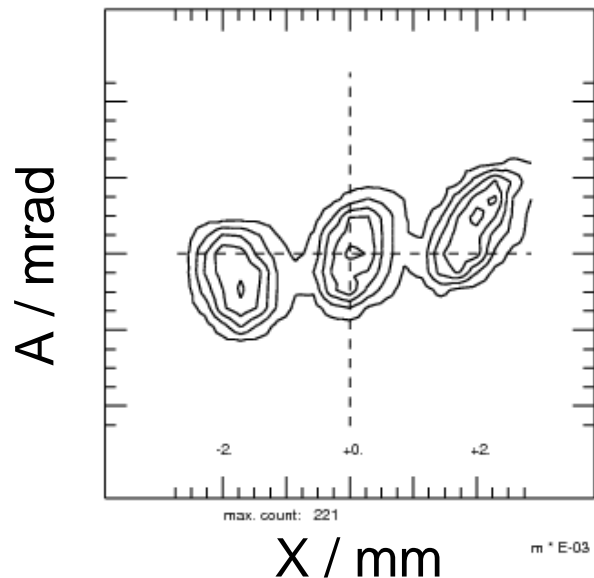
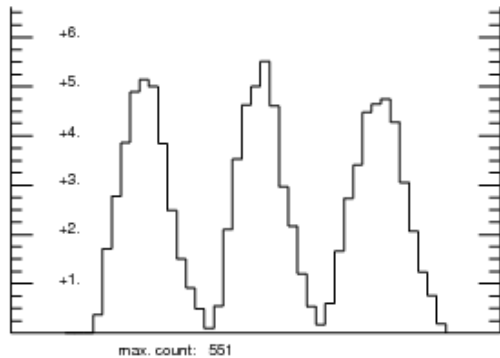
1st- 3rd quad rot. by 1°



Similar result for rotation of quadrupoles behind dipoles

Rotation in 1st module can be compensated by 3rd

1st- 3rd quad rot. by 0.5°



Well aligned and adjusted system

$$(X,B) = 0, (X,Y) = 0,$$

and

$$(X,AA) = 0$$

1st+ 3rd quad rot. by 1°
Size of contributions

$$(X,B) * B_0 = -0.56 \text{ mm}$$

(for $B_0 = 10 \text{ mrad}$)

but also ($X_0 = Y_0 = 0.5 \text{ mm}, A_0 = 7 \text{ mrad}$)

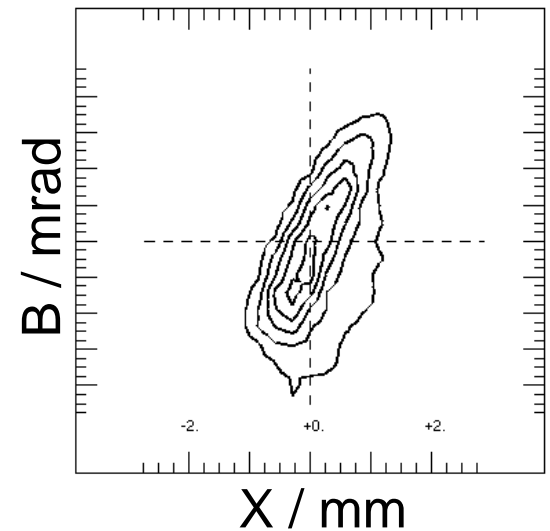
$$(X,AA) * A_0 * A_0 = 0.28 \text{ mm}$$

$$(X,AY) * A_0 * Y_0 = 0.41 \text{ mm}$$

$$(X,AB) * A_0 * B_0 = -0.19 \text{ mm}$$

$$(X,YY) * Y_0 * Y_0 = 0.24 \text{ mm}$$

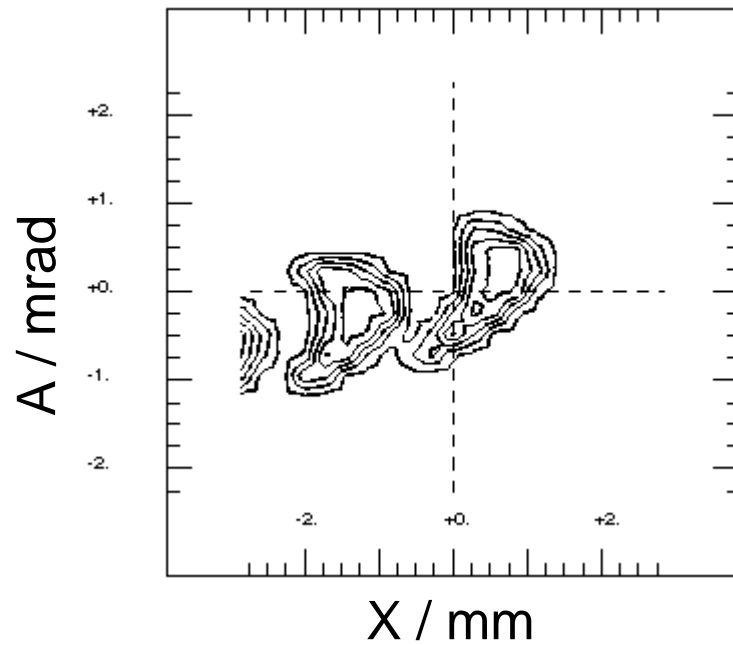
numbers are maximal values not peak widths



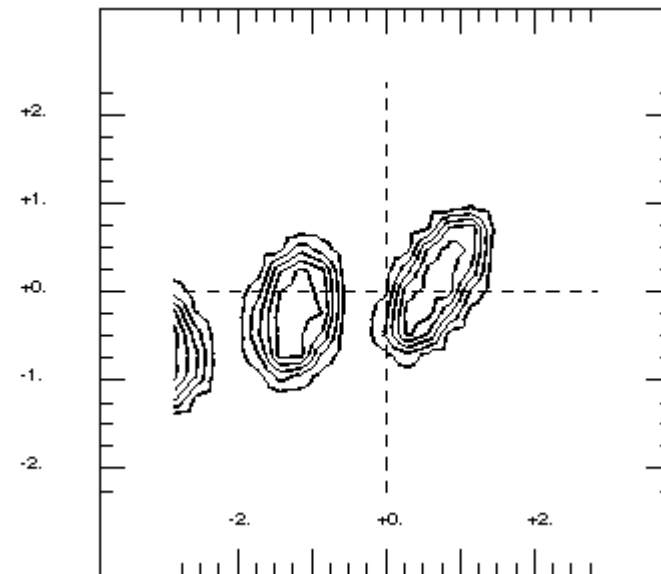
Influence of Shifts, X

1st module shifted by $\Delta x = 0.1\text{mm}$

old hexapole value



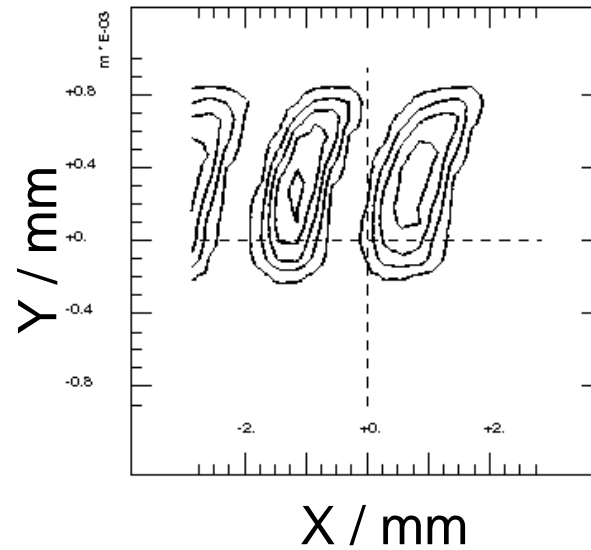
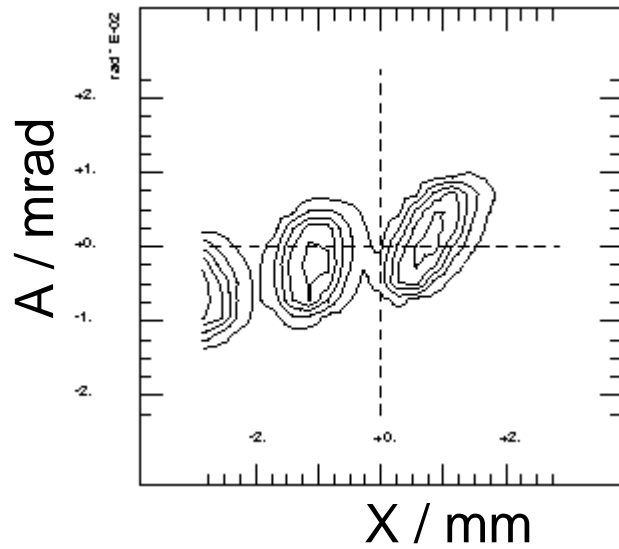
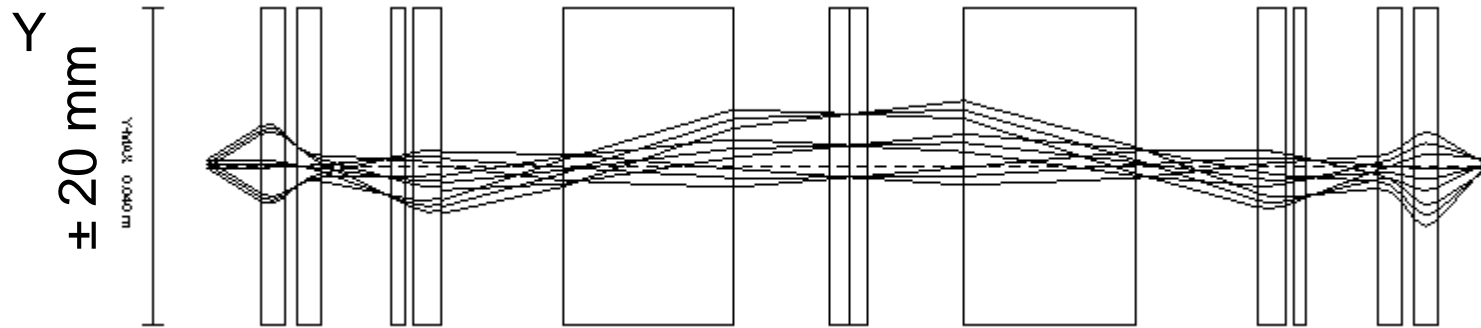
hexapole +1.4%



(X,AA) and some (X,BB),(X,XA)

Influence of Shifts, Y

1st module shifted by $\Delta x = 0.1\text{ mm}$, $\Delta y = 0.5\text{ mm}$



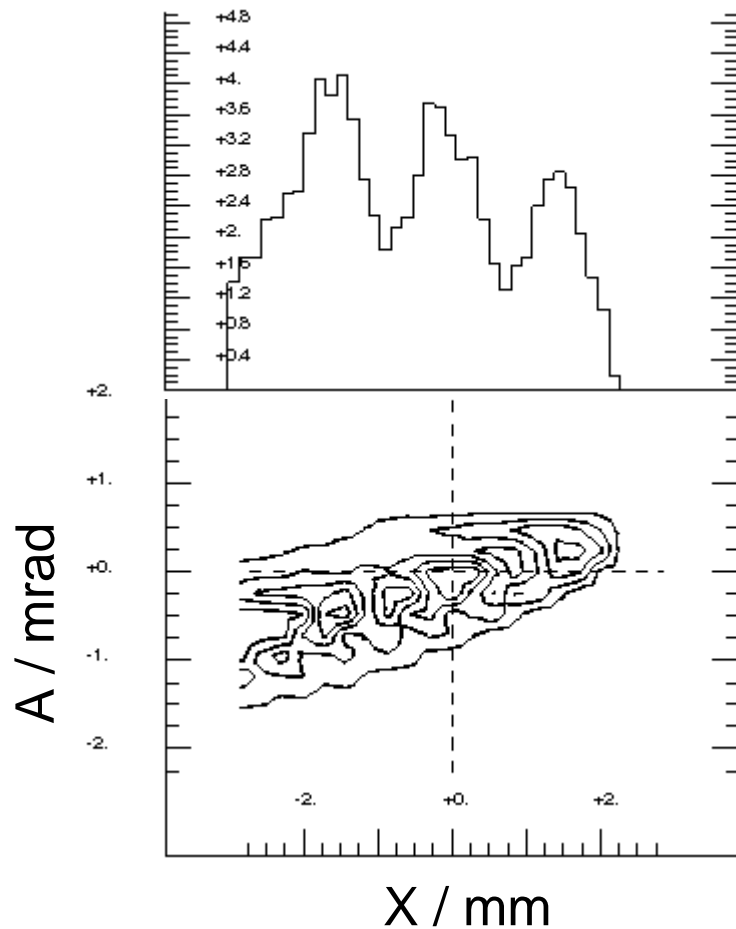
some (X,Y)

X, Y independent
for small shifts

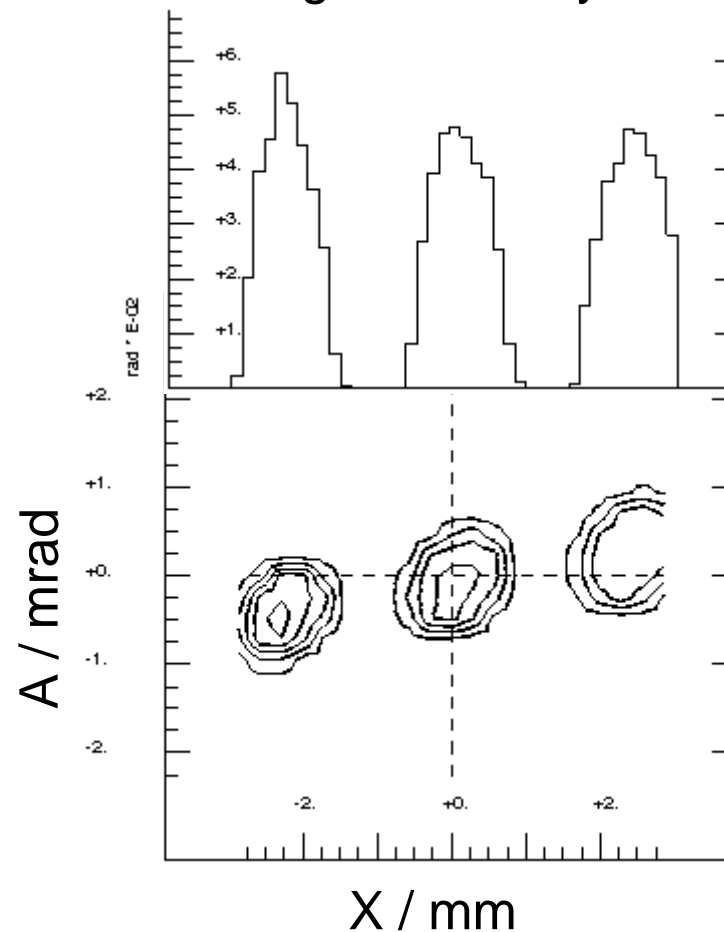
Initial Beam Direction

Angle in y is uncritical, but angle in X is critical.

assume $\Delta A = 1$ mrad
uncompensated



assume $\Delta A = 1$ mrad, but
central multipole hex +10% and
final image shifted by $\Delta z = 14$ cm



For even larger shifts use steerers